## Discounting Effectiveness

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## What are we talking about?

A class of decision problems characterized by:
$>$ multiyear profile
$>$ importance of timeliness
$>$ changing effectiveness
Examples might include:
$\square$ adding R\&D capacity
$\square$ developing an in-house capability
$\square$ building strategic partnerships
But we're going to talk about some boats...

## Once upon a threat...

A small island nation faces two maritime threats:
$>$ sea-based smuggling of luxury goods

- reducing tax revenue
$>$ fishery predation by foreign fishing fleets
- jeopardizing food supply

To counter these threats, the government has decided to procure and operate a fleet of Offshore Patrol Vessels (OPV). Two types of vessel are available, A and B.

## Cost-effectiveness

## Common approach to C-E Analysis

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## Comparing alternatives

Suppose we apply these models and determine:

$$
\begin{aligned}
& \mathrm{MOE}_{\mathrm{A}}=0.5 \\
& \mathrm{MOE}_{\mathrm{B}}=0.6 \\
& \operatorname{Cost}_{\mathrm{A}}=\$ 52 \mathrm{M} \\
& \operatorname{Cost}_{\mathrm{B}}=\$ 57 \mathrm{M}
\end{aligned}
$$

## Two important issues

Issue 1 We are comparing a discounted LCC with a non-discounted MOE
Not a problem if timing is not a concern
Issue 2 MOE is representative for a single vessel in a "head-to-head" comparison
Not a problem if the MOE of $k$-many vessels is $k$ times the MOE of one.

## Effectiveness over time...

Think about building up a level of effectiveness over time (proxied by number of vessels operating).


## A fleet effectiveness function

Consider a (pure) fleet MOE function of the form:


## Back to our two OPVs

Suppose that $\mathrm{MOE}_{\mathrm{A}}=0.5$ and $\mathrm{MOE}_{\mathrm{B}}=0.6$. Further suppose that:
$>$ A is available for procurement next year at a rate of 2 vessels per year.
$>\mathrm{B}$ will not available to procure for two years, but can be procured at a rate of 3 vessels per year.

For simplicity, we assume that personnel and maintenance constraints will limit the final fleet to 10 vessels of a single type.

## Fleet effectiveness over time

Production of fleet effectiveness over time under the assumption that $\alpha=2$ and $\beta=6$.

|  | Type A OPVs |  |  | Type B OPVs |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | Procure | Operate | $\boldsymbol{f}()$. | Procure | Operate | $\boldsymbol{f}()$. |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 2 | 0 | 0 | 0 | 0 | 0 |
| 2 | 2 | 2 | 0.054 | 3 | 0 | 0 |
| 3 | 2 | 4 | 0.199 | 3 | 3 | 0.139 |
| 4 | 2 | 6 | 0.393 | 3 | 6 | 0.451 |
| 5 | 2 | 8 | 0.589 | 1 | 9 | 0.741 |
| 6 | 0 | 10 | 0.751 | 0 | 10 | 0.811 |
| 7 | 0 | 10 | 0.751 | 0 | 10 | 0.811 |
| 8 | 0 | 10 | 0.751 | 0 | 10 | 0.811 |
| 9 | 0 | 10 | 0.751 | 0 | 10 | 0.811 |
| 10 | 0 | 10 | 0.751 | 0 | 10 | 0.811 |

## Fleet effectiveness over time

Graphic depiction of fleet effectiveness over time


## Marginal effectiveness over time

Marginal increases of fleet effectiveness over time


## Effectiveness decreases over time


$r_{t}$ represents a measure of effectiveness lost due to a one period delay in operation of a vessel.

## Tradeoffs

Tradeoffs: "... an OPV operational in year $t$ is worth $\gamma_{t}$ as much as one operational in year $t+1 \ldots$ "

Behavior: Given the existence of a threat, it's reasonable to assume the decision maker's preference is to have vessels operational sooner rather than later, so $\gamma_{\mathrm{t}} \geq 1 \forall \mathrm{t}$.

## Tradeoffs $\rightarrow$ discount rates



## Discounting example

## Stronger desire for rapid deployment:

| Year | $\Delta \mathbf{E}\left(\mathbf{A}, \mathrm{n}_{\mathrm{t}}\right)$ | $\Delta_{\mathbf{E}}\left(\mathbf{B}, \mathbf{n}_{\mathfrak{t}}\right)$ | $\gamma_{t}$ | $\mathrm{r}_{\mathrm{t}}$ | Discount Factor | $\underset{\mathbf{d}^{\Delta} \mathbf{E}(\cdot)}{\text { OPV A }}$ | $\underset{\mathbf{d}^{\Delta} \mathbf{E}(\cdot)}{\text { OPV B }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 4 | 3 |  |  |  |
| 1 | 0 | 0 | 3 | 2 | 0.2500 | 0 | 0 |
| 2 | 0.0540 | 0 | 3 | 2 | 0.0833 | 0.0045 | 0 |
| 3 | 0.1452 | 0.1393 | 2 | 1 | 0.0278 | 0.0040 | 0.0039 |
| 4 | 0.1942 | 0.3119 | 2 | 1 | 0.0139 | 0.0027 | 0.0043 |
| 5 | 0.1954 | 0.2896 | 2 | 1 | 0.0069 | 0.0014 | 0.0020 |
| 6 | 0.1618 | 0.0704 | 1 | 0 | 0.0035 | 0.0006 | 0.0002 |
| 7 | 0 | 0 | 1 | 0 | 0.0035 | 0 | 0 |
| 8 | 0 | 0 | 1 | 0 | 0.0035 | 0 | 0 |
| 9 | 0 | 0 | 1 | 0 | 0.0035 | 0 | 0 |
| 10 | 0 | 0 | 1 | 0 | 0.0035 | 0 | 0 |
|  | 0.7506 | 0.8111 |  |  |  | 0.0132 | 0.0105 |
| Undiscounted MOE |  |  |  |  |  | Discounted MOE |  |

## Discounting example

## Lesser desire for rapid deployment:

| Year | $\Delta \mathbf{E}\left(\mathbf{A}, \mathrm{n}_{\mathrm{t}}\right)$ | $\Delta^{\mathbf{E}}\left(\mathbf{B}, \mathbf{n}_{\mathfrak{t}}\right)$ | $\gamma_{t}$ | $\mathrm{r}_{\mathrm{t}}$ | Discount Factor | $\underset{\mathbf{d}^{\Delta} \mathbf{E}(\cdot)}{\text { OPV A }}$ | $\underset{\mathbf{d}^{\Delta} \mathbf{E}(\cdot)}{\text { OPV B }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 3 | 2 |  |  |  |
| 1 | 0 | 0 | 2 | 1 | 0.3333 | 0 | 0 |
| 2 | 0.0540 | 0 | 1.5 | 0.5 | 0.1667 | 0.0090 | 0 |
| 3 | 0.1452 | 0.1393 | 1 | 0 | 0.1111 | 0.0161 | 0.0155 |
| 4 | 0.1942 | 0.3119 | 1 | 0 | 0.1111 | 0.0216 | 0.0347 |
| 5 | 0.1954 | 0.2896 | 1 | 0 | 0.1111 | 0.0217 | 0.0322 |
| 6 | 0.1618 | 0.0704 | 1 | 0 | 0.1111 | 0.0180 | 0.0078 |
| 7 | 0 | 0 | 1 | 0 | 0.1111 | 0 | 0 |
| 8 | 0 | 0 | 1 | 0 | 0.1111 | 0 | 0 |
| 9 | 0 | 0 | 1 | 0 | 0.1111 | 0 | 0 |
| 10 | 0 | 0 | 1 | 0 | 0.1111 | 0 | 0 |
|  | $0.7506$ | $0.8111$ |  |  |  | 0.0864 | 0.0901 |
| Undiscounted MOE |  |  |  |  |  | Discounted MOE |  |

## C-E consequences




Lesser desire for rapid deployment MB/MC required

## Benefits

$>$ Provides a framework to examine consequences of time preferences
$>$ Can be used to examine consequences of:

- Obsolescence (technology, threat, etc.)
- Changes in mission/strategy
- Developing capabilities over time
- Anything affecting MOE at the margin


## Caveats

$>$ Infinite postponement and immediate consumption (Keeler and Cretin 1993)

Rely on constant discount rates and perfect exchangeability of present and future money and benefits (Chapman and Elstein 1995)

- Employ a time varying vice a constant discount rate (Harvey 1994)
- Perfect exchangeability is not feasible in defense (threat and budgeting)


## Caveats

$>$ A discounting approach can induce a short-run focus and lead decision makers to always favor upgrading existing systems rather than investing in new ones. This can increase risks in the future.

- In the OPV example, a fleet of 7 type C vessels with $\mathrm{MOE}_{\mathrm{C}}=0.1$ available for immediate procurement is preferred to either fleet of 10 type A or 10 type B vessels due to their delay.


## That's all, folks!

